1.	A medical researcher is studying the relationship between age (x years) and volume
	of blood (y ml) pumped by each contraction of the heart. The researcher obtained the
	following data from a random sample of 8 patients.

Age (x)	20	25	30	45	55	60	65	70
Volume (y)	74	76	77	72	68	67	64	62

[You may use
$$\sum x = 370$$
, $S_{xx} = 2587.5$, $\sum y = 560$, $\sum y^2 = 39418$, $S_{xy} = -710$]

(a) Calculate S₁₃

(2)

(b) Calculate the product moment correlation coefficient for these data.

(2)

(c) Interpret your value of the correlation coefficient.

(1)

The researcher believes that a linear regression model may be appropriate to describe these data.

- (d) State, giving a reason, whether or not your value of the correlation coefficient supports
 the researcher's belief.
- (e) Find the equation of the regression line of y on x, giving your answer in the form y = a + bx (4)

Jack is a 40-year-old patient.

- (f) (i) Use your regression line to estimate the volume of blood pumped by each contraction of Jack's heart.
 - (ii) Comment, giving a reason, on the reliability of your estimate.

c) stong evidence to suggest negative correlation exists. The older a person the lower the volume

3. A biased four-sided die has faces marked 1, 3, 5 and 7. The random variable X represents the score on the die when it is rolled. The cumulative distribution function of X, F(x), is given in the table below.

x	4	3	5	7
F(x)	0.2	0.5	0.9	ι

(a) Find the probability distribution of X

(b) Find P(2 < $X \le 6$)

(2)

(4)

(c) Write down the value of F(4)

(1)

The random variable Y ~ N(μ, σ²)
 Given that P(Y < 17) = 0.6 find

(a) P(Y > 17)

(b) $P(\mu < Y < 17)$

(2)

(c) $P(Y < \mu | Y < 17)$

a) P(4717) = 467 - = 0.40

/X - 401.

P(M(Y(17) = 0.10

b) D(= 7 17-14) = 407.

e	table	below	shows	the	distances	(to	the	nearest	km)	travelled	to	work 1	by	the 5	50
ıp	loyees	in an	office.												

Distance (km)	Frequency (f)	Distance midpoint (x)
0-2	16	1.25
3 – 5	12	25th 4
6-10	10 3	8
11 – 20	8	15.5
21 – 40	4	30.5

[You may use
$$\sum fx = 394$$
, $\sum fx^2 = 6500$]

A histogram has been drawn to represent these data.

The bar representing the distance of 3-5 has a width of 1.5 cm and a height of 6 cm.

- (a) Calculate the width and height of the bar representing the distance of 6-10(3)
- (b) Use linear interpolation to estimate the median distance travelled to work.
- (c) (i) Show that an estimate of the mean distance travelled to work is 7.88 km.
 - (ii) Estimate the standard deviation of the distances travelled to work. (4)
- (d) Describe, giving a reason, the skewness of these data.

Peng starts to work in this office as the 51st employee.

She travels a distance of 7.88 km to work.

(e) Without carrying out any further calculations, state, giving a reason, what effect

Peng's addition to the workforce would have on your estimates of the

(i) mean,

2. The

em

- (ii) median,
- (iii) standard deviation

of the distances travelled to work.

(2)

(2)

(3)

$$F \gtrsim 12$$
 $j \div 4$
 $F \gtrsim 12$ $j \div 4 \times 3$
 $A = 7 \cdot 5 \cdot m^2$
 $\therefore h = 3 \cdot cm$

Ci)
$$\bar{x} = \frac{2fx}{x} = \frac{394}{50} = 7.88$$

ii)
$$Sxx = 6500 - 394^{2} \div 50 = 3395.28 P = \int 5xx = 8.24$$

d) Mean (7.88) > Maken (4-75) : positre chem

iii) Slight reduction $E(x-\bar{x})$ unchanged but a how increased by 1.

x	-2	0	2	4	
P(X=x)	a	ь	а	с	1
where a, b and c are	e probabilities.				\
Given that $E(X) = 0$	0.8				1
a) find the value	of c.				(2)
Given also that E($(X^2) = 5$ find				
b) the value of a	and the value o	f <i>b</i> ,			2.4
	*				(4)
c) Var(X)					(2)
he random variab	le Y = 5 - 3X				
ind					
d) E(Y)					(1)
e) Var(Y)					(2)
f) $P(Y \ge 0)$					(4)
a) E(x)=	- 2a + 2	a+4c	:0-8 :	. c=0.	
) E(x')	= 40+	ta+16c	= 5 80	= 1.8 0	=0.
E1 = 1	=) 2a+	b+c=1	- 5=	0.35	
) V(x)= 6				-	
) V(S-3* P(Y>O):)= 9V(x	() = 29.2	4 1141	(-2x)= S	-3(0
, ,,,,	- 15 0	117	, a) o (5 5 7 5	2.6

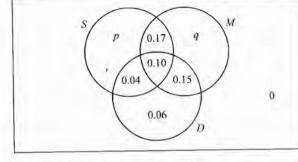
tennis ball is modelled by a normal distribution with mean 32 m and standard deviation 12 m. Any child who throws the tennis ball more than 50 m is awarded a gold certificate. (a) Show that, to 3 significant figures, 6.68% of children are awarded a gold certificate. A silver certificate is awarded to any child who throws the tennis ball more than d metres but less than 50 m. Given that 19.1% of the children are awarded a silver certificate, (b) find the value of d. Three children are selected at random from those who take part in the throwing a tennis ball event. (c) Find the probability that 1 is awarded a gold certificate and 2 are awarded silver certificates. Give your answer to 2 significant figures. 0=12 P(d>50)=P(Z>50-32) 41 = P(Z>1-S)=1-Q(1-S) b) P(D>d)=0.191+0.868 = 0.2578 - 0 (d) = 0-7422 d= 0.65 b) P(2 > d-32) = 0.191 +0.0668 = 0.2578 = Q(d-32)= 0-7422 : d-32 = 065 :- d = 39.8m GSS X3 = 3×0.0668×0.1912 0.06731

7. One event at Pentor sports day is throwing a tennis ball. The distance a child throws a

(4)

6. The Venn diagram below shows the probabilities of customers having various combinations of a starter, main course or dessert at Polly's restaurant.

$$S$$
 = the event a customer has a starter.



Given that the events S and D are statistically independent

- (a) find the value of p.
- (b) Hence find the value of q.
- (c) Find
 - (i) $P(D \mid M \cap S)$
 - and their extent of
 - (ii) $P(D \mid M \cap S')$

One evening 63 customers are booked into Polly's restaurant for an office party. Polly has asked for their starter and main course orders before they arrive.

(4)

(2)

(4)

(2)

Of these 63 customers

- 27 ordered a main course and a starter,
- 36 ordered a main course without a starter.
- (d) Estimate the number of desserts that these 63 customers will have.

a)
$$P(S) \times P(O) = P(S \times O)$$
 (0.31+p) $\times 0.3S = 0.14$
 $\Rightarrow P = 0.09$
b) $Q = 1 - ... = 0.39$
C) i) $P(D|MAS) = 0.10 = 0.37$
ii) $P(D|MAS') = 0.1S = 0.278$
O) $\Rightarrow P(D|MAS') = 0.1S = 0.278$
d) $\Rightarrow P(D|MAS') = 0.1S = 0.278$